

TEST 2

Time: 70min

1. Evaluate $\int e^\theta \cos \theta d\theta$.
2. For which natural numbers n , does the approximation $MID(n)$ give the exact value of $\int_0^{2\pi} \sin \theta d\theta$. Compute $MID(1)$, $MID(2)$, and $MID(3)$.
3. If during an epidemic people get sick at the rate of $r(t) = 1000te^{-0.5t}$, how many people get sick altogether.
4. Find the volume of the solid obtained by revolving the region bounded by $y = x^3$, $x = 1$, and $y = -1$ around the axis $y = -1$.
5. A rod of length of 3 with density $\delta(x) = 1 + x^2$ is positioned along the positive x -axis, with its left end at the origin. Find the mass and the center of mass of the rod.
6. **(Extra Credit)** Calculate the escape velocity of an object from the earth.

Each problem is worth 10 pts.